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The Phase Equilibria and Crystal Chemistry of the Intermediate Phases in the Ytterbium-Antimony System¹

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Seven stable intermediate phases have been found to exist in the ytterbium-antimony system. YbSb_2 is orthorhombic, Cmcm , and is isostructural with ZrSi_2 ; YbSb is fcc and has the NaCl structure with $a = 6.082$ Å; two phases having the 5:4 stoichiometry exist with the $\alpha \rightarrow \beta$ transition occurring at 1030° . The low-temperature form, $\alpha\text{-Yb}_5\text{Sb}_4$, is tetragonal, I^{42}_m , with $a = 11.90$ Å and $c = 17.06$ Å. The high-temperature form, $\beta\text{-Yb}_5\text{Sb}_4$ is orthorhombic, Pnma or $\text{Pn}2_1a$, with $a = 8.13$ Å, $b = 15.97$ Å, and $c = 24.39$ Å. The phase Yb_4Sb_3 is bcc, $I\bar{4}3d$, with $a = 9.320$ Å, and has the anti-thorium phosphide, Th_3P_4 , structure. The alloy Yb_5Sb_3 is hexagonal, P^3/mcm , with $a = 8.995$ Å and $c = 6.870$ Å and is isostructural with Mn_5Si_3 . The phase richest in ytterbium is Yb_6Sb_2 , orthorhombic, $\text{Pn}2_1a$, with $a = 12.32$ Å, $b = 9.60$ Å, and $c = 8.32$ Å. Two phases, YbSb_2 and Yb_4Sb_3 , melt congruently at 945 and 1540° , respectively. The β form of Yb_5Sb_4 melts incongruently at 1400° while YbSb decomposes at 820° . The remaining phases, Yb_5Sb_3 and Yb_6Sb_2 , melt incongruently at 1520 and 1400° , respectively, but loss of ytterbium vapor occurs at the melting point indicating vapor-solid equilibrium in this region of the phase diagram.

Introduction

Ytterbium displays divalent and trivalent oxidation states in its compounds and similar behavior can be expected to occur in intermediate phases formed between it and semimetals such as antimony and bismuth. McMasters and Gschneidner² investigated the Yb-Mg system and found that ytterbium displays divalent character throughout the diagram. The intermediate phase YbSb has been reported by Iandelli³ and Brixner,⁴ and the phases YbSe and YbTe have been reported by Senff and Klemm,⁵ all of these are isostructural with NaCl. As part of a program dealing with the study of rare earth-group Va and VIa systems, the phase diagram, crystal chemistry, and magnetic susceptibility of the intermediate phases found in the Yb-Sb system have been investigated in order to determine whether the oxidation state of the rare earth atom varies in these alloys and what, if any, correlation exists between observed bond lengths in the different phases and their magnetic moments. This paper discusses the phase diagram and crystal chemistry of the system and the results of the magnetic measurements and discussion of the oxidation states of ytterbium will be published elsewhere.

Experimental Section

Ytterbium metal of 99.9% purity was obtained from the Nuclear Corp. of America and antimony of 99.99% purity was obtained from Johnson, Mathey and Co. Samples of appropriate composition of the elements were sealed in tantalum tubes under several millimeters of argon and allowed to react. The lower melting phases YbSb_2 , YbSb , and $\alpha\text{-Yb}_5\text{Sb}_4$ were prepared by heating at 800° for 3-4 days in conventional resistance furnaces capable of reaching 1200° and holding at $\pm 5^\circ$. In this procedure the tantalum ampoules were again sealed into large Vycor tubes to prevent oxidation of the tantalum tubes. Quench-

ing of samples from the resistance furnaces was accomplished by dropping the tubes into ice water or brine. Quenching times of 2-5 sec were obtained. Intermediate phases with higher melting points ($\beta\text{-Yb}_5\text{Sb}_4$, Yb_4Sb_3 , Yb_5Sb_3 , and Yb_6Sb_2) were allowed to react for shorter periods to reduce the reaction of antimony with tantalum. Reaction times of 2-5 min in a vacuum induction furnace at $1100\text{-}1600^\circ$ were found to be satisfactory. Quenching in the induction furnace was not as rapid since there was no means to remove heat suddenly. However, temperature drops of 1000° could be obtained in less than 1 min. All sample annealing was done in tantalum tubing at temperatures approximating 75% of the melting points.

Single-crystal and powder X-ray diffraction techniques were used to identify the phases. Microscopic examination was also used to determine the nature of the quenched samples. Density measurements were made by the displacement technique using acetone as the liquid. Melting points were measured by a procedure previously described.⁶

Single-crystal X-ray diffraction data were collected for YbSb_2 , Yb_4Sb_3 , and Yb_5Sb_3 to confirm the crystal structures and to obtain more accurate values for the bond distances. Small crystals of irregular shape were selected for each phase. No absorption corrections were applied and isotropic temperature factors were used in all instances. Crystal structure determinations are now in progress on the intermediate phases whose structures are unknown.

Results

Phase Diagram.—A proposed equilibrium phase diagram for the Yb-Sb system is presented in Figure 1. Solid lines represent regions elucidated by a study of quenched samples and the dashed lines represent uncertain areas. The symbols denote observations made on quenched samples. No efforts were made to determine the eutectic points precisely, nor was the solubility at the terminal ends of the diagram studied.

The study of this binary system was complicated by the extreme volatility of the ytterbium metal. Large pressures were developed inside the tantalum tubes during the reaction, and these made pressure an active thermodynamic variable. Except for Yb_5Sb_3 , the reaction pressures were probably less than 1 atm at reaction temperatures near 1000° . The pressures de-

(1) Research sponsored by National Science Foundation Grant GP-2029.

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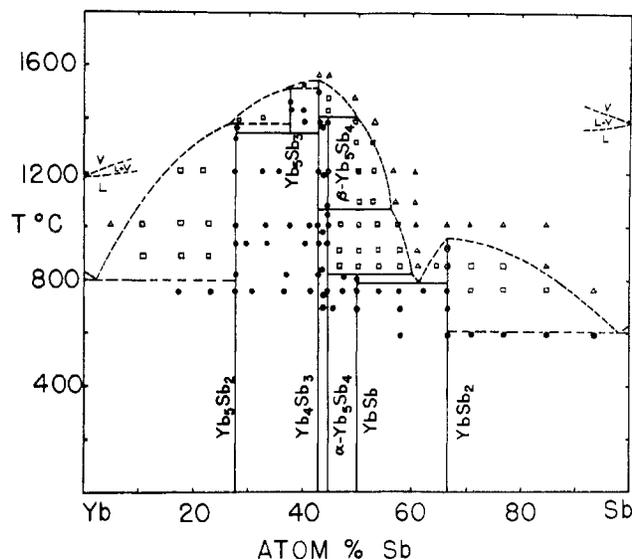


Figure 1.—Proposed phase diagram for the system Yb-Sb: O, single-phase solid; ●, two-phase solid; □, liquid and solid; Δ, liquid.

veloped in producing Yb_5Sb_3 around 1400° were more than 1 atm as evidenced by the bulging of the tantalum reaction containers. Since the boiling points of the elements are quite low, they are included on the diagram along with the initial portion of the liquid-vapor loop for both elements. A linear behavior would lead to the intersection of the vapor-liquid loop with the liquid-solid region resulting in vapor-solid equilibrium. Sublimation rather than melting of Yb_5Sb_2 and Yb_5Sb_3 was observed when their melting points were determined.

Further difficulty was encountered because of a violent exothermic reaction which occurred near 600° as the sample containers were heated to the normal reaction temperatures. This behavior dispersed the elemental constituents on the walls of the container and thereby prevented the establishment of equilibrium conditions. This effect was reduced significantly by compacting the reaction mixtures into pellets and also by heating very slowly across this temperature range.

X-Ray diffraction powder patterns of quenched samples richer in Sb than 66.7 atom % showed YbSb_2 and Sb in equilibrium. YbSb_2 was found to melt congruently at $845 \pm 15^\circ$. Samples with Sb compositions between 50 and 66.7 atom % which had reacted below 800° showed that YbSb and YbSb_2 were in equilibrium. Quenched samples between 820 and 1130° showed no sign of YbSb , but a mixture of liquid and either $\alpha\text{-Yb}_5\text{Sb}_4$ or YbSb_3 , depending on the composition. Samples near 60 atom % Sb when slow-cooled across the 800° isotherm showed YbSb and YbSb_2 in approximately a 2:1 ratio, indicating a eutectic point near 60%. The $\alpha\text{-Yb}_5\text{Sb}_4$ composition was obtained at 44.4 atom % Sb, and samples with slightly less antimony showed $\alpha\text{-Yb}_5\text{Sb}_4$ and Yb_4Sb_3 in equilibrium below 1030° and those with slightly more antimony showed $\alpha\text{-Yb}_5\text{Sb}_4$ and YbSb in equilibrium below 820° ; transformation to $\beta\text{-Yb}_5\text{Sb}_4$ occurred above 1030° . The phase $\beta\text{-$

Yb_5Sb_4 could also be produced from the elements in the correct proportion above 1030° and it melted incongruently at $1400 \pm 25^\circ$.

The phase Yb_4Sb_3 was produced at temperatures ranging from 800 to 1400° although the optimum condition for synthesis was near 1000° . It melts congruently at $1540 \pm 10^\circ$ and the vapors leaving the molten liquid when condensed on a cold glass slide were still of the same structure and composition as the original solid. The compound Yb_5Sb_3 was produced at temperatures above 1350° and appeared to exist in equilibrium with Yb vapor. At $1520 \pm 10^\circ$, loss of Yb resulted in the formation of Yb_4Sb_3 . Specimens of Yb_5Sb_3 were stable at room temperature but when heated above 1100° would dissociate to Yb_4Sb_3 and Yb_5Sb_2 . It was impossible to produce homogeneous samples of Yb_5Sb_3 below 1350° .

The best single-phase material of the phase richest in Yb was at the 28.6 atom % Sb composition. It could be produced at temperatures ranging from 825 to 1300° although loss of Yb from volatilization was more serious at elevated temperatures. The phase Yb_5Sb_2 releases Yb vapors when heated in open containers above 1000° , and at 1400° it is completely dissociated. From density and volume considerations, each unit cell contains 30 atoms, but at a 5:2 composition, this would imply partial atom occupancy. It is possible that a range of homogeneity exists for this phase, but no attempt was made in the present work to determine composition variability.

The element Yb is normally face-centered cubic and has a phase transition to body-centered cubic at 720° . We have also observed a phase transition to a hexagonal close-packed structure which was stable above 300° and thus ytterbium also displays the structure in which all the other rare earth elements in the latter half of the series crystallize. The lattice parameters $a = 3.855 \text{ \AA}$ and $c = 6.280 \text{ \AA}$ are consistent with the size anomaly usually encountered with Yb. The hexagonal form has also been reported by Spedding, *et al.*,⁷ who considered it an impurity-stabilized phase, where the contaminant is oxygen or nitrogen, and by Stephens,⁸ who reports its presence in Yb which was at least 99.86 wt % pure.

Crystal Data

The crystallographic and physical parameters are summarized in Table I; X-ray powder diffraction data are shown in Table II. Lattice constants for YbSb_2 , YbSb , Yb_4Sb_3 , and Yb_5Sb_3 were obtained by measurements of powder diffraction lines in the back-reflection region and plotting those values against $\sin^2 \theta$. Extrapolation to $\sin^2 \theta = 1$ yielded the values shown in Table I and they are considered accurate to $\pm 0.002 \text{ \AA}$. The other phases had powder patterns that were too complex and the lines in the back reflection region cannot be indexed unambiguously; the lattice constants for these phases are accurate to $\pm 0.01 \text{ \AA}$.

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son, and Tharp¹¹ report Sm_5Ge_4 with similar space group and cell constants. The cell constants for $\beta\text{-Yb}_5\text{Sb}_4$ are $a = 8.13$ A, $b = 15.97$ A, and $c = 24.39$ A. The c parameter appears to be 8.13 A, but close examination of X-ray photographs reveals faint reflections which can be attributed to a supercell made by tripling the original c parameter of 8.13 A. This was not observed for Sm_5Ge_4 , but might be related in this case to the mechanism of the phase transformation from $\alpha\text{-Yb}_5\text{Sb}_4$ to $\beta\text{-Yb}_5\text{Sb}_4$. This supercell was observed on crystals obtained both by direct synthesis of the elements and by the phase transformation from $\alpha\text{-Yb}_5\text{Sb}_4$. The crystal structure of this phase is currently under investigation.

Yb_4Sb_3 .—This phase crystallizes in the *anti*-thorium phosphide, Th_3P_4 , structure. Similar *anti*- Th_3P_4 structures have been reported by Holtzberg¹² and Hohnke and Parthe¹³ for 4:3 composition of lanthanides with group IV and V elements. The Th_3P_4 structure is characterized by one variable positional parameter in the space group $\text{I}\bar{4}3\text{d}$, associated in this case with the Yb atoms. The least-squares refinement of 36 general hkl reflections obtained photographically with Mo $\text{K}\alpha$ radiation yielded a value of 0.074 ± 0.001 for the positional parameter. Ideal atomic packing would result in a parameter of 0.083, but the presence of both covalent and ionic bonding displaces the Yb atoms from the ideal position. A value of 0.0745 was obtained by Cox, *et al.*,¹⁴ for La_2Te_3 , and Holtzberg, *et al.*,¹⁵ report a positional parameter of 0.0715 for Gd_2Se_3 and 0.075 for La_3Se_4 . The compounds Gd_2Se_3 and La_2Te_3 contain vacancies whereas La_3Te_4 does not. The Yb–Sb bond distances in Yb_4Sb_3 are 3.139 and 3.323 A, the two separations resulting from the displacement of the Yb atom from the idealized position. No variation in stoichiometry commonly observed for the regular Th_3P_4 -type structure was observed for Yb_4Sb_3 .

Yb_5Sb_3 .—This phase crystallizes with the manganese silicide, Mn_5Si_3 , structure, D_8_3 type. The variable atomic positions obtained by a least-squares refinement of 70 $h\bar{k}0$ and $h0l$ reflections obtained photographically with Cu $\text{K}\alpha$ radiation are shown in Table III.

TABLE III

Atom	x	$\sigma(x)$	y	z
4-Yb(I)	0.333	...	0.667	0
6-Yb(II)	0.2516	0.0010	0	0.250
6-Sb	0.6115	0.0016	0	0.250

The Yb(I)–Sb bond distances are 3.272 A for the nearly octahedral Sb coordination around the Yb(I)

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atoms at a fixed position. Two of the Yb(II)–Sb bond distances are 3.240 A, and the third is 3.068 A. This short distance is probably due to the very anisotropic coordination of Yb(II) by the antimony atoms. The sublimation of ytterbium from Yb_5Sb_3 at elevated temperatures is probably due to the loss of Yb(II) atoms which are clustered at the corners of the unit cell.

The Mn_5Si_3 structure has been reported for stannides and plumbides of all of the lanthanides except europium and ytterbium by Jeitschko and Parthe.¹⁶ It appears that the structure is influenced by the number of valence electrons present, and the shortage for Yb is overcome by a trivalent element such as antimony. No other rare earth–group V 5:3 alloys have been reported, and the narrow temperature range may indicate that this phase is not very stable.

Yb_5Sb_2 .—This phase is richest in ytterbium and crystallizes in an orthorhombic structure with the probable space group $\text{Pn}2_1\text{a}$. A crystal structure determination has been undertaken and a proposed structure has been reported.¹⁷ There appear to be atoms with statistical occupancy in the unit cell, and this agrees with the partial atom occupancy referred to earlier.

Discussion

There are seven stable intermediate phases in the system, some of which are isotypic with known structures and others have new structures. YbSb_2 appears to be the first ZrSi_2 -type structure in these rare earth–intermetallic systems. The NaCl structure for YbSb is typical of all of the equimolar group V and VI lanthanides. The *anti*- Th_3P_4 structure for Yb_4Sb_3 has been previously reported for other group V–rare earth alloys of this composition, but the variable positional parameter of 0.074 is less than the idealized parameters of $1/12$ or 0.083. New structures also exist for $\alpha\text{-Yb}_5\text{Sb}_4$, $\beta\text{-Yb}_5\text{Sb}_4$, and Yb_5Sb_2 . Yb_5Sb_3 appears to be the first Mn_5Si_3 structure reported for a rare earth–group V alloy.

The only other rare earth–antimony system reported is the La–Sb system investigated by Vogel and Klose.¹⁸ Although no crystal structures are given, the phases LaSb_2 , LaSb , La_3Sb_2 , and La_2Sb are reported. Since then, Hohnke and Parthe¹³ report La_4Sb_3 with the *anti*- Th_3P_4 structure. LaSb_2 has been reported by Wang¹⁹ to have a new structure closely related to YbSb_2 . The La_2Sb structure is probably related to Yb_5Sb_2 , but has not been confirmed.

Ytterbium, with the dual oxidation state, exhibits the size anomaly associated with the divalent state for Yb_4Sb_3 when compared to other RE_4Sb_3 alloys. The lack of anomalous behavior for YbSb suggests trivalent Yb behavior in this alloy and this has been reported by Iandelli.³

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